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Modeling the optimal compensation capacitance of a giant magnetostrictive ultrasonic transducer with a loosely-coupled contactless power transfer system

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Abstract: The giant magnetostrictive rotary ultrasonic processing system (GMUPS) with a loosely-coupled contactless power transfer (LCCPT) has emerged as a high-performance technique for the processing of hard and brittle materials, owing to its high power density. A capacitive compensation is required to achieve the highest energy efficiency of GMUPS to provide sufficient vibration amplitude when it works in the resonance state. In this study, an accurate model of the optimal compensation capacitance is derived from a new electromechanical equivalent circuit model of the GMUPS with LCCPT, which consists of an equivalent mechanical circuit and an electrical circuit. The phase lag angle between the mechanical and electrical circuits is established, taking into account the non-negligible loss in energy conversion of giant magnetostrictive material at ultrasonic frequency. The change of system impedance characteristics and the effectiveness of the system compensation method under load are analyzed. Both idle vibration experiments and machining tests are conducted to verify the developed model. The results show that the GMUPS with optimal compensation capacitance can achieve the maximum idle vibration amplitude and smallest cutting force. In addition, the effects of magnetic conductive material and driving voltages on the phase lag angle are also evaluated.

Key words: Rotary ultrasonic machining; Giant magnetostrictive transducer (GMT); Loosely-coupled contactless power transfer (LCCPT); Electromechanical equivalent circuit; Optimal compensation capacitance

1 Introduction

Hard and brittle materials, represented by ultrahigh temperature ceramics and ceramic matrix composites, play a vital role in the aerospace field but they are generally difficult to process using traditional methods. Rotary ultrasonic machining (RUM) is a superior processing technology that applies ultrasonic vibration to the tool to improve the processing performance. The RUM has many advantages in processing hard and brittle materials, including high efficiency, high geometrical accuracy, low cutting heat, long tool life, and low cutting force (Gong et al., 2010; Liu et al., 2012; Wang Y et al., 2014; Wang JJ et al., 2016, 2021). In

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Received July 27, 2022; Revision accepted Aug. 23, 2022; Crosschecked Sept. 23, 2022 addition, it is well known that, in RUM, within an amplitude range, the larger the ultrasonic amplitude, the better the processing effect (Liu et al., 2019). The ultrasonic transducer is the crucial component of an RUM system. The transducer that converts the electrical energy into mechanical vibration is usually made of piezoelectric materials.

In addition to piezoelectric materials, giant magnetostrictive material (GMM) emerges as a new and promising energy-converting material for RUM systems. The GMM has the characteristics of high electromechanical conversion efficiency, high power density, and high-quality factor. It can output larger amplitudes with less power and volume (Zhang et al., 2004). The giant magnetostrictive rotary ultrasonic processing system (GMUPS), which uses GMM as the transducer material, can achieve a larger amplitude, and thus a higher material processing efficiency than traditional RUM systems (Zeng, 2013; Cai et al., 2017b).

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When performing RUM, the transducer of GMUPS needs to rotate at high speed along with the tool, so it is necessary to use a non-contact method to power the transducer. Using a rotary transformer composed of a pair of coils as a loosely-coupled contactless power transfer (LCCPT) device is usually adopted for power transmission. However, since non-contact power transmission devices will bring a specific inductive load, compensation capacitance is needed to achieve the most efficient energy transmission and maximize amplitude output. Much related research has been done on piezoelectric systems (Jiang and Zhang, 2007; Pang, 2010; Huang and Paramo, 2011; Shen et al., 2015; Zhang, 2019). However, the energy conversion form in the GMM transducer is more complicated than that in the piezoelectric transducer (Zhou et al., 2020b; Ma et al., 2022). The GMUPS needs to be compensated by a unique method. In the past, the compensation methods usually regarded the minimum current frequency as the mechanical resonance frequency and compensated it for electrical resonance (Cai et al., 2017a; Fan et al., 2019). However, these methods have significant deviations, which cause unnecessary energy loss and affect the system's stability.

The unnecessary energy loss that occurs in GMUPS is mainly caused by the core loss (including hysteresis loss and eddy current loss) and skin effect during energy transfer, due to the energy conversion method of the electricity-magnetism-mechanism. These will induce a phase lag between the system's mechanical and electrical parts, indicating a low energy utilization efficiency (Calkins, 1997). In the past, most GMMs were operated at low frequencies, such as sonar systems (Chen, 2015), linear motors (Claeyssen et al., 1997), pumps (Chen et al., 2014), and actuators (Zhang et al., 2004). In those applications, although the core loss and skin effect of GMMs have an impact, they are not as significant as at the ultrasonic frequency. Wakiwaka et al. (1992) found that the phase lag angle between the equivalent mechanical circuit and the electrical circuit was slight under their experimental frequency of 925 Hz. Thus, the phase lag angle caused by the unnecessary energy loss is usually ignored in low-frequency operations because of its small value.

However, in GMUPS, the phase lag angle is much higher than that in low-frequency systems and cannot be ignored. According to research on the performance of metal materials (Wang et al., 2004), both the hysteresis and eddy current losses and the skin effect will cause phase lag in an alternating magnetic field. GMM has essentially the same electromagnetic properties as traditional metal materials, and so the most direct causes of the phase lag are the skin effect and core loss that occur when the GMM and the magnetic permeability material transmit an alternating magnetic field. Since both the core loss and the loss caused by the skin effect increase with frequency, the unnecessary energy loss is significant at high frequencies. The phase lag angle caused by unnecessary energy loss is also significant, and its impact on the system cannot be ignored. Therefore, when analyzing GMUPS, the influence of the phase lag angle must be considered. Zhou et al. (2021) reported a significant difference between the minimum current frequency and the mechanical resonance frequency in GMUPS. This discovery shows that the phase lag angle is significant in the ultrasound system, and a unique compensation method must be used for GMUPS.

In this study, an optimum compensation capacitance model of GMUPS with LCCPT was developed, taking into account the phase lag angle between the mechanical and electrical parts of the system. Combined with the equivalent physical model of cutting load, the load's influence on the performance of capacitance compensation was analyzed. The vibration amplitude measurement without load and drilling experiments were carried out at different compensation capacitances to verify the model. Finally, the effect factors of the phase lag angle were analyzed.

2 Modeling the optimal compensation capacitance

In this section, the electromechanical equivalent circuit model of the GMUPS using LCCPT is first constructed by considering the phase lag angle between the equivalent mechanical circuit and the electrical circuit. Then, the constructed circuit model is mapped using the equivalent method, and the equation of optimal compensation capacitance is derived through the mapped circuit. Finally, the effects of the compensation capacitance on the vibration amplitude of the system under no-load and under loaded conditions are analyzed.

2.1 Illustration of GMUPS structure with LCCPT

The GMUPS, as shown in Fig. 1, can be divided into five parts: giant magnetostrictive transducer (GMT), holder, horn, tool, and LCCPT. The transducer converts alternating current (AC) electrical signals into high-frequency vibration to output mechanical energy. The transducer mainly includes excitation coils, magnetic conductors, permanent magnets, and GMM. The GMM is sliced to reduce eddy current loss and skin effect. The tool holder connects the transducer and the machine tool so that the transducer can rotate together with the machine tool. The horn is used to amplify the amplitude of the mechanical vibration output by the transducer and transmit it to the tool for material processing. The LCCPT is used to provide power to the rotary ultrasonic transducer.



Fig. 1 Structure of GMUPS with LCCPT

The LCCPT includes two parts, the primary and the secondary coil devices. The primary coil is fixed on the machine tool and does not rotate during machining. The secondary coil is fixed on the tool holder housing and rotates with the transducer. A very narrow air gap exists between them, forming an LCCPT through mutual inductance. The primary coil is directly connected with the ultrasonic power supply, and the secondary coil is connected with the excitation coil inside the transducer. The electronic energy is transmitted through electromagnetic induction from the primary to the secondary coil. However, their inductive reactance will affect the system's impedance, limiting the ultrasonic power and vibration amplitude. Therefore, a suitable compensation circuit is essential to maintain the performance of GMUPS (including amplitude, efficiency, and temperature rise).

2.2 Phase lag angle between the mechanical and electrical circuits

To accurately compensate for the electrical resonance, the electromechanical equivalent circuit model of GMUPS needs to be constructed. For the GMT, the electromechanical equivalent circuit is shown in Fig. 2a (Wakiwaka et al., 1992). The left circuit is the electrical circuit, and the right circuit is the equivalent mechanical circuit. U is the voltage, R_1 is the resistance of the electrical circuit, L_1 is the inductance of the electrical circuit, and C_1 is the compensation capacitance when the LCCPT is not in use. F is the equivalent force, and v is the equivalent velocity of the system.



Fig. 2 (a) Electromechanical equivalent circuit without LCCPT and (b) dynamic impedance circle without LCCPT

The impedances of the mechanical part of the electromechanical equivalent circuit of the transducer can be expressed as shown in (Wakiwaka et al., 1992).

When the load stress is less than the proof stress, the strain ε is proportional to the stress σ . The final value of the strain is determined by the modulus of elasticity and obeys Hooke's law:

$$R_{\rm m} = c = 2m\pi (f_2 - f_1),$$

$$L_{\rm m} = m, \ C_{\rm m} = \frac{1}{k} = \frac{1}{4\pi f_{\rm m}^2 m},$$
(1)

where C_m is the mechanical equivalent capacitance, L_m is the mechanical equivalent inductance, R_m is the mechanical equivalent resistance, *m* is the mass of the transducer, f_1 and f_2 are the half power frequencies on the impedance circle, *c* is the equivalent damping of the system, *k* is the equivalent stiffness of the system, and f_n is the mechanical resonance frequency of the system.

There will be a phase lag between the equivalent mechanical circuit and the electrical circuit, due to unnecessary energy loss in energy conversion. For GMUPS, there are two resonance frequencies. One is the mechanical resonance frequency, which is the frequency corresponding to the maximum amplitude; the other is the electrical resonance frequency when the circuit is resistive. Because of the phase lag, the minimum current frequency is not equal to the mechanical resonance frequency, and there is a deviation of tens of Hertz between these two frequencies. Thus, in actual use, we need to compensate the circuit at the mechanical resonance frequency.

Considering the phase lag between the equivalent mechanical and electrical circuits, the electromechanical equivalence coefficient T_{em} shown in Fig. 2a can be expressed as a complex, i.e.,

$$T_{\rm em} = R_{\rm em} + jX_{\rm em} = \sqrt{R_{\rm em}^2 + X_{\rm em}^2} e^{j\beta},$$

$$\tan \beta = \frac{X_{\rm em}}{R_{\rm em}}, \ T_{\rm em}^2 = (R_{\rm em}^2 + X_{\rm em}^2) e^{j2\beta},$$
(2)

where R_{em} is the real part of T_{em} , X_{em} is the imaginary part of T_{em} , and β is the angle between the real part and the imaginary part.

The phase lag angle is 2β , which is between the mechanical equivalent circuits and the electrical circuits. It can be used to characterize the deviation of the minimum current frequency and the mechanical resonance frequency in the impendence cycle (Zhou et al., 2021). Fig. 2b shows the dynamic impedance circle without LCCPT. The X'O'R' is the dynamic impedance coordinate system and r_{emut} is the radius of

the dynamic impedance circle. Due to the influence of the phase lag angle, the transducer cannot achieve mechanical resonance when working at the minimum current frequency.

2.3 Derivation of optimal compensation capacitance model

When using LCCPT, the difference between the mechanical and electrical resonance frequencies is affected by the inductance of the coils in addition to the phase lag angle. To maximize the energy conversion efficiency and the maximum output amplitude of the GMUPS, the mechanical resonance and electrical resonance need to occur at the same frequency. Therefore, a compensation capacitance needs to be connected in series between the system power supply and the LCCPT to adjust the electrical resonance frequency. Moreover, the modeling of optimum compensation capacitance needs to consider the influence of the phase lag angle and the use of LCCPT.

Finding the optimal compensation capacitance requires an accurate electromechanical equivalent circuit to obtain accurate system impedance. The traditional mapping method usually maps the equivalent mechanical circuit to the resistor-inductor-capacitor (RLC) parallel circuit. But this mapping method does not consider T_{em} as a complex number with a phase lag angle. In this study, as shown in Fig. 3, the equivalent mechanical circuit is mapped to an RLC series circuit, and the combination of equivalent capacitance and equivalent inductance is regarded as equivalent reactance. This method can eliminate the modeling error caused by the phase lag angle.

The electromechanical equivalent circuit model of GMUPS with LCCPT is shown in Fig. 3a. The left circuit is the primary circuit of LCCPT, the middle circuit is the secondary circuit of LCCPT, and the right circuit is the equivalent mechanical circuit. R_e and L_e are the resistance and inductance of the primary coil of LCCPT, respectively. C_e is the compensation capacitance on the primary circuit, M is the mutual inductance of the LCCPT, R_s and L_s are the resistance and inductance of the secondary coil of LCCPT, respectively, R_e is the resistance of the excitation coil, and L_e is the inductance of the excitation coil.

The circuit mapping is performed in two steps. In the first step, the right circuit that corresponds to the



Fig. 3 Electro-mechanical equivalent circuit and the mapping circuits: (a) original circuit; (b) circuit after first mapping; (c) circuit after second mapping. Explanations of parameters are given in the following sections

equivalent mechanical circuit is mapped to the middle circuit, as shown in Fig. 3b. In Fig. 3b, R_{\circ} is the combined resistance of the excitation coil and transducer, and X_{\circ} is the combined reactance of the excitation coil and transducer. R_{gmut} and X_{gmut} are the resistance and reactance of the mechanical mapping, respectively, and Z_{gmut} is the impedance of the mechanical mapping. They are calculated by the following equations:

$$Z_{gmut} = R_{gmut} + jX_{gmut} = \frac{T_{em}^2}{Z_m},$$

$$Z_m = R_m + j\omega L_m + \frac{1}{j\omega C_m},$$

$$R_{gmut} = \frac{(R_{em}^2 - X_{em}^2)R_m + 2R_{em}X_{em}\left(\omega L_m - \frac{1}{\omega C_m}\right)}{R_m^2 + \left(\omega L_m - \frac{1}{\omega C_m}\right)^2}, \quad (3)$$

$$X_{gmut} = \frac{2R_{em}X_{em}R_m - (R_{em}^2 - X_{em}^2)\left(\omega L_m - \frac{1}{\omega C_m}\right)}{R_m^2 + \left(\omega L_m - \frac{1}{\omega C_m}\right)^2},$$

where ω is the angular frequency.

Among them, in Fig. 3b, take the resistance of the new right circuit as R_{see} , the reactance of the new right circuit as X_{see} , and the overall impedance of the new right circuit as Z_{see} , then:

$$Z_{\text{sec}} = R_{\text{sec}} + jX_{\text{sec}}, \quad R_{\text{sec}} = R_{\text{s}} + R_{\text{c}} + R_{\text{gmut}},$$

$$X_{\text{sec}} = \omega L_{\text{s}} + \omega L_{\text{c}} + X_{\text{gmut}}.$$
(4)

In the second step, the new right circuit is mapped to the primary circuit, as shown in Fig. 3c. To facilitate calculations, it is also mapped to an RLC series circuit to obtain the overall equivalent reactance and resistance. In Fig. 3c, R_{mot} and X_{mot} are the mapped resistance and reactance of the new right circuit, respectively, and Z_{mot} is the impedance of the new right circuit. They can be calculated by the following equations:

$$Z_{\rm mot} = \frac{\omega^2 M^2}{Z_{\rm sec}} = \frac{\omega^2 M^2}{R_{\rm sec} + jX_{\rm sec}} = \frac{\omega^2 M^2 (R_{\rm sec} - jX_{\rm sec})}{R_{\rm sec}^2 + X_{\rm sec}^2},$$

$$X_{\rm mot} = -\frac{\omega^2 M^2 X_{\rm sec}}{R_{\rm sec}^2 + X_{\rm sec}^2}, \quad R_{\rm mot} = \frac{\omega^2 M^2 R_{\rm sec}}{R_{\rm sec}^2 + X_{\rm sec}^2}.$$
(5)

When the GMUPS works at the mechanical resonance frequency,

$$\omega_{\rm n}L_{\rm m} - \frac{1}{\omega_{\rm n}C_{\rm m}} = 0, \qquad (6)$$

where ω_n is the mechanical resonance angular frequency, and $\omega_n = 2\pi f_n$.

Then, R_{sec} and X_{sec} can be expressed as

$$R_{sec|\omega_{s}} = R_{s} + R_{c} + \frac{R_{em}^{2} - X_{em}^{2}}{R_{m}} =$$

$$R_{s} + R_{c} + 2r_{gmut} \cos(2\beta),$$

$$X_{sec|\omega_{s}} = \omega L_{s} + \omega L_{c} + \frac{2R_{em}X_{em}}{R_{m}} =$$

$$\omega L_{s} + \omega L_{c} + 2r_{gmut} \sin(2\beta).$$
(7)

In the dynamic impedance circle,

$$\tan \alpha_{\omega_{n}} = \frac{X_{\text{sec}|\omega_{n}}}{R_{\text{sec}|\omega_{n}}} = -\frac{\omega_{n}L_{s} + \omega_{n}L_{c} + 2r_{\text{gmut}}\sin(2\beta)}{R_{s} + R_{c} + 2r_{\text{gmut}}\cos(2\beta)}, \quad (8)$$

where α_{ω_a} is the phase lag angle between the primary circuit and the mechanical equivalent circuit in Fig. 3a, which differs from the lag phase angle 2β when

LCCPT is not used. This difference is caused by the resistance and inductance of the primary and secondary coils of LCCPT.

From Fig. 3 and Eq. (5), the overall reactance of the system is

$$X = X_{\text{mot}} + X_{\text{e}} = X_{\text{mot}} + \omega L_{\text{e}} - \frac{1}{\omega C_{\text{e}}}$$

$$= \omega L_{\text{e}} - \frac{1}{\omega C_{\text{e}}} - \frac{\omega^2 M^2 X_{\text{sec}}}{R_{\text{sec}}^2 + X_{\text{sec}}^2}.$$
(9)

When electrical resonance occurs, the overall reactance is zero. When mechanical resonance and electrical resonance occur at the same time,

$$X_{\omega_{n}} = \omega_{n} L_{e} - \frac{1}{\omega_{n} C_{o}} - \frac{\omega_{n}^{2} M^{2} X_{\sec(\omega_{n})}}{R_{\sec(\omega_{n})}^{2} + X_{\sec(\omega_{n})}^{2}} = 0, \quad (10)$$

where C_{\circ} is the optimal compensation capacitance. Substituting Eqs. (2) and (7) into Eq. (10) and simplifying it, we can obtain an expression for C_{\circ} as follows:

$$C_{o} = \frac{1}{\left\{\omega_{n}^{2}L_{e} - \omega_{n}^{3}M^{2}\left(\omega_{n}L_{s} + \omega_{n}L_{e} + \frac{2R_{em}^{2}\tan\beta}{R_{m}}\right)\right/}{\left[\left(R_{s} + R_{e} + \frac{R_{em}^{2} - R_{em}^{2}\tan^{2}\beta}{R_{m}}\right)^{2} + \left(\omega_{n}L_{s} + \omega_{n}L_{e} + \frac{2R_{em}^{2}\tan\beta}{R_{m}}\right)^{2}\right]\right\}.$$
(11)

2.4 Performance analysis of optimal compensation capacitance with/without load

Since the optimal compensation capacitance is determined at the mechanical resonance frequency, which is directly affected by the cutting force, the performance of optimal compensation capacitance needs to be analyzed for both no-load and loaded conditions. A theoretical model is developed to analyze the effects of compensation capacitance on the vibration amplitude of GMUPS.

For a general GMUPS, the amplitude prediction models under no-load and loaded conditions were obtained in our previous studies (Zhou et al., 2019, 2020a), respectively, and the amplitude models were:

$$A = \frac{QM_{\rm LT}LI_{\rm a}}{\sqrt{\left[Q(1-h^2)\right]^2 + h^2}}, A' = \frac{\alpha'I_{\rm a}}{\sqrt{\left(1 - \frac{f^2}{f_{\rm n}'^2}\right)^2 + \left(\frac{2\varsigma f}{f_{\rm n}'}\right)^2}},$$
(12)

where A is the idle ultrasonic amplitude, A' is the ultrasonic amplitude under load, I_a is the drive current, Q is the quality factor of the system, M_{LT} is the amplification factor of the horn, L is the length of the GMM, h is the ratio of the driving frequency to the resonance frequency, ζ is the system damping, α' is the system amplitude coefficient, f is the driven frequency, and f_n' is the mechanical resonance frequency of the system under load.

According to Eqs. (3)–(5), the impedance circle equation of the GMUPS with LCCPT can be obtained:

$$\begin{bmatrix} R - \left(R_{e} + R_{\omega_{n}}\right) \end{bmatrix}^{2} + \begin{bmatrix} X - \left(\omega L_{e} - \frac{1}{\omega C_{e}} + X_{\omega_{s}}\right) \end{bmatrix}^{2} = r_{\text{mot}}^{2}, \\ R_{\omega_{n}} = \omega_{n}^{2} M^{2} \left(R_{s} + R_{c} + \frac{R_{\text{em}}^{2} - X_{\text{em}}^{2}}{R_{m}}\right) \times \\ \left\{ 2 \left[\left(R_{s} + R_{c} + \frac{R_{\text{em}}^{2} - X_{\text{em}}^{2}}{R_{m}}\right)^{2} + \left(\omega_{n} L_{s} + \omega_{n} L_{c} + \frac{2R_{\text{em}} X_{\text{em}}}{R_{m}}\right)^{2} \right] \right\}^{-1}, \\ X_{\omega_{n}} = -\omega_{n}^{2} M^{2} \left(\omega_{n} L_{s} + \omega_{n} L_{c} + \frac{2R_{\text{em}} X_{\text{em}}}{R_{m}}\right)^{2} + \left(\omega_{n} L_{s} + \omega_{n} L_{c} + \frac{2R_{\text{em}} X_{\text{em}}}{R_{m}}\right)^{2} + \left(\omega_{n} L_{s} + \omega_{n} L_{c} + \frac{2R_{\text{em}} X_{\text{em}}}{R_{m}}\right)^{2} \right] \right\}^{-1}, \\ r_{\text{mot}}^{2} = \omega_{n}^{4} M^{4} \times \left[\left(R_{s} + R_{c} + \frac{R_{\text{em}}^{2} - X_{\text{em}}^{2}}{R_{m}}\right)^{2} + \left(\omega_{n} L_{s} + \omega_{n} L_{c} + \frac{2R_{\text{em}} X_{\text{em}}}{R_{m}}\right)^{2} \right]^{-1}, \end{cases}$$

where r_{mot} is the radius of the dynamic impedance circle, R_{ω_n} and X_{ω_n} are the mapped resonance resistance

and reactance of the secondary circuit and equivalent mechanical circuit, respectively.

Combining Eqs. (7), (12), and (13), the relationship between the vibration amplitudes and compensation capacitance can be obtained:

$$A = \frac{QM_{LT}L}{\sqrt{\left[Q(1-h^{2})\right]^{2} + h^{2}}} \times \frac{U_{a}}{\frac{\omega^{2}M^{2}(R_{sec} - jX_{sec})}{R_{sec}^{2} + X_{sec}^{2}} + R_{e} + j\omega L_{e} + \frac{1}{j\omega C_{e}}},$$

$$A' = \frac{\alpha'}{\sqrt{\left(1 - \frac{f^{2}}{f_{n}'^{2}}\right)^{2} + \left(\frac{2gf}{f_{n}'}\right)^{2}}} \times \frac{U_{a}}{\frac{\omega^{2}M^{2}(R_{sec} - jX_{sec})}{R_{sec}^{2} + X_{sec}^{2}} + R_{e} + j\omega L_{e} + \frac{1}{j\omega C_{e}}},$$
(14)

where U_a is the drive voltage.

Fig. 4 shows the system's resonant amplitude under no-load and loaded conditions for different compensation capacitances, which are obtained through Eq. (14). Under no-load conditions, the resonance amplitude of the system first increases and then decreases with the compensation capacitance. The resonance amplitude reaches its maximum value under the optimal compensation capacitance. When the system is under load, the no-load optimal compensation capacitance can still achieve the maximum amplitude and maintain the best machining performance. In summary, the optimal compensation capacitance is still adequate for the operation of GMUPS under load.

3 Experimental verification

A series of experiments was conducted under no-load and loaded conditions to evaluate the validity of the optimal compensation capacitance model. Firstly, the parameters of the transducer were identified to calculate the theoretical value of the optimal compensation capacitance. Then, idle vibration measurement tests for different compensation capacitances were carried out to verify the developed model under no-load condition. Finally, drilling experiments were performed to evaluate the performance of the optimal compensation capacitance under loaded condition.



Fig. 4 Idle resonance frequency amplitude curve of the system with different compensation capacitance (a) and resonance amplitude with different compensation capacitance under load (b)

3.1 Obtaining optimal compensation capacitance

To calculate the optimal compensation capacitance, it is necessary to obtain the required parameters through measurements, including the basic electrical parameters of the GMUPS, the mechanical resonance frequency, and the other variables included in Eq. (11), such as R_{em} and β . The parameter identification experiments of the transducer were conducted on a selfdesigned GMUPS, which is mounted on a computerized numerical control (CNC) lathe (DMG CTX310, DMG, Germany). The experimental platform is shown in Fig. 5. The basic electrical parameters of GMUPS with LCCPT were measured by a multimeter with results listed in Table 1.

The mechanical resonance frequencies of GMUPS, with and without LCCPT, can be derived from the amplitude-frequency curves of the system, which were measured using a laser displacement sensor





Fig. 5 Experimental setup of displacement measurement: (a) process and measurement part; (b) control part

Table 1 Dasic parameters of Giv	NUPS
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Parameter	Value
$L_{\rm e}$ (mH)	1.94
$L_{\rm s}$ (mH)	1.82
M (mH)	1.18
$R_{\rm s}(\Omega)$	2.20

(LK-H008, Keyence, Japan) with a sampling rate of 392 kHz with a revolution of 0.01 μ m. The measurement results of amplitude-frequency curves are shown in Fig. 6. The mechanical resonance frequencies are 19640 Hz in both cases with and without LCCPT. However, after using LCCPT, the system's electrical circuit has changed significantly, which induces a distinct electrical resonance frequency compared with the system without LCCPT. Therefore, although there is a coupling between the mechanical and electrical parts of the system, the mechanical resonance frequency are independent. Thus, mechanical and electrical resonances can be considered separately in the study of ultrasonic systems.

According to Eq. (11), R_{em} and β are also needed to calculate the optimal compensation capacitance and



Fig. 6 Amplitude-frequency curve of GMUPS with and without LCCPT

can be obtained by measuring the impedance circle when the LCCPT is not used. However, calculating $R_{\rm em}$ and β by measuring the impedance circle needs a large amount of data to fit the impedance circle; the calculation process is very complicated. So other, less complicated approaches are needed and are described as follows.

We combine the impedance of the excitation coil with the equivalent impedance of the transducer obtained by the first equivalent circuit mapping (Fig. 3b) as

$$X_{o} = X_{c} + X_{gmut} = X_{ms} + \frac{1}{\omega C_{s}}, R_{o} = R_{c} + R_{gmut} = R_{ms}, \quad (15)$$

where $R_{\rm ms}$ is the equivalent resistance of the system when the LCCPT is not used, $X_{\rm c}$ is the reactance of the excitation coil, and $X_{\rm ms}$ is the equivalent reactance of the system when the LCCPT is not used.

Substituting Eqs. (7) and (15) into Eq. (11) and simplifying, the optimal compensation capacitance can be expressed as follows:

$$C_{o} = \frac{1}{\omega_{n}^{2}L_{e} - \frac{\omega_{n}^{3}M^{2}\left(\omega_{n}L_{s} + X_{ms} + \frac{1}{\omega_{n}C_{1}}\right)}{\left(R_{s} + R_{ms}\right)^{2} + \left(\omega_{n}L_{s} + X_{ms} + \frac{1}{\omega_{n}C_{1}}\right)^{2}}.$$
(16)

According to Eq. (16), the optimal compensation capacitance can be calculated after obtaining C_1 , X_{ms} , and R_{ms} . X_{ms} and R_{ms} can be obtained by measuring the mechanical resonant current and the mechanical resonant voltage through the power meter (PW3335,

HIOKI, Japan) when the LCCPT is not used. According to Eq. (15) and Figs. 2a and 3, C_1 is only an intermediate variable when calculating C_0 . Different values of C_1 will change X_{ms} , but will not change X_0 and R_0 . Theoretically, therefore, C_1 does not affect C_0 .

However, we can use C_1 to calculate C_o more accurately by carrying out experiments at different values of C_1 . Experiments were conducted at different C_1 of 50, 60, 65, 70, 75, 80, 90, and 100 nF using the PW3335 power meter and power supply (BP4610, NF, Japan). The measurement results of X_{ms} and R_{ms} are listed in Table 2. By substituting X_{ms} and R_{ms} into Eq. (13), the optimal compensation capacitance C_o is calculated with the results listed in Table 2. It should be noted that C_1 does not exist in the final actual circuit, and it is only used in the process of solving C_o . Taking the average value of C_o in Table 2, the optimal compensation capacitance is obtained as 46.10 nF.

Table 2 Theoretical value of C_{a}

C_1 (nF)	$R_{ m ms}\left(\Omega ight)$	$X_{ m ms}\left(\Omega ight)$	$C_{o}(\mathrm{nF})$
50	49.43	-54.62	46.25
60	49.45	-28.89	46.32
65	45.69	-16.88	46.29
70	48.08	-1.93	46.05
75	46.18	5.53	46.02
80	46.22	12.37	45.99
90	50.03	23.99	45.92
100	51.77	31.60	45.96

3.2 Performance of optimal compensation capacitance without load

The performance of the GMUPS with the optimal compensation capacitance under no-load conditions was evaluated using the device shown in Fig. 5. Firstly, the amplitude-frequency curves under different compensation capacitances of 40, 45, 48, and 51 nF were measured with results shown in Fig. 7a. The maximum amplitude under all compensation capacitance is around 19640 Hz, and does not change with the compensation capacitance. This phenomenon further illustrates that the electrical and mechanical properties of the system are independent of each other. Therefore, the relationship curve between resonance amplitude and compensation capacitance can be measured at 19640 Hz to obtain the optimal value of compensation capacitance. The measurement results are shown in Fig. 7b.



Fig. 7 Amplitude-frequency curve of different compensation capacitances (a) and relationship curve between resonance amplitude and compensation capacitance (b)

The GMUPS with optimal compensation capacitance shows much-improved resonance performance for no-load conditions. The shape of the resonance amplitude-compensation capacitance curve has a high similarity to the theoretical curve (Fig. 4a). The resonance amplitude first increases and then decreases with the compensation capacitance. The resonance amplitude reaches its maximum value of 10.9 μ m around the theoretical value of optimal compensation capacitance of 46.1 nF. These experimental results verify the efficacy of the developed model of optimal compensation capacitance.

The GMUPS can work at both mechanical and electrical resonances simultaneously when the optimal compensation capacitance is utilized. The amplitudefrequency and phase-frequency curves were measured with results shown in Fig. 8. As demonstrated in Fig. 8, the frequency corresponding to the zero-phase point coincides with the frequency of maximum amplitude.



Fig. 8 Results of the resonance experiment with optimal compensation capacitance

Thus, the electrical resonance and mechanical resonance co-occur. In this circumstance, the system works with maximum energy utilization efficiency. It should be noted that in the resonance experiment, the phase response of the system reaches zero at several driving frequencies. However, the ultrasonic system can achieve the maximum vibration amplitude at only one of the zero-phase frequencies (Jiang and Zhang, 2007).

3.3 Performance of optimal compensation capacitance during drilling

A series of drilling experiments was performed to verify the effectiveness of the optimal compensation capacitance under load. The experimental setup is shown in Fig. 9. The GMUPS with LCCPT is fixed using a three-jaw chuck to achieve the rotary motion. The workpiece is fixed on the tool holder to provide the feeding motion. The workpiece material is quartz ceramic. The drilling experiment uses a carbide tool with a diameter of 6 mm. It is electroplated with diamond abrasive grains with mesh size of 120/140. The spindle speed of 3000 r/min and the feed rate of 5 mm/min were used for drilling experiments. A dynamometer (9256C2, Kistler, Switzerland) was used to measure the cutting force during the drilling process with a sampling rate of 1000 Hz.

Fig. 9b shows the variation of cutting force for a complete drilling process. Since this experiment uses an external cutting fluid, it becomes more difficult for the cutting fluid to work as the drilling depth increases, and thus the cutting force increases with the drilling depth. Therefore, when discussing the compensation effect of different compensation capacitances, it is



Fig. 9 Drilling platform (a) and cutting force variation during drilling with the compensation of 46.1 nF (b)

sufficient to compare the cutting force at the beginning stage and the finishing stage. It can be obtained from Fig. 7b that the compensation capacitances corresponding to the half-power points are 40.7 and 52.5 nF. Thus, two points around the half-power band are selected as controls. The compensation capacitances of 0, 41.0, 46.1, 51.0, and 100.0 nF were used for drilling experiments, with results shown in Fig. 10.

The GMUPS with optimal compensation capacitance also works well during machining. Fig. 10 shows the cutting force at the beginning and finishing stages using the GMUPS with different compensation capacitances. Under the optimal compensation capacitance (46.1 nF), the cutting forces for both the beginning and finishing stages reach the smallest values. It is well recognized that the cutting force decreases with the ultrasonic amplitude in RUM (Wang et al., 2020). Thus, in Fig. 10, a smaller cutting force indicates a larger ultrasonic amplitude, which is consistent with the variation trend of resonant amplitude in Fig. 7. The experimental results are in accordance with the



Fig. 10 Results of the drilling experiments

4 Effect factors of the phase lag angle

The optimal compensation capacitance is directly related to the phase lag angle, as shown in Eq. (11). The phase lag angle greatly affects the performance of GMUPS. To study the effect factors of the phase lag angle, it is first necessary to obtain the equation of the phase lag angle. Substituting Eqs. (1), (2), and (5) into Eq. (16) and simplifying, β can be obtained by solving Eq. (17) as follows:

$$R_{\rm em} X_{\rm em} = m\pi (f_2 - f_1) \left(X_{\rm ms} + \frac{1}{\omega C_{\rm s}} - X_{\rm c} \right),$$

$$R_{\rm em}^2 - X_{\rm em}^2 = 2m\pi (f_2 - f_1) (R_{\rm ms} - R_{\rm c}),$$
 (17)

$$\beta = \arctan \frac{X_{\rm em}}{R_{\rm em}}.$$

According to Eq. (17), β can be calculated after obtaining X_{em} and R_{em} . X_{em} and R_{em} can be obtained by measuring X_{ms} , R_{ms} , and the equivalent electrical parameters of GMUPS. It is worth noting that the change of the mechanical resonance frequency under different driving voltages is only tens of Hertz, which is very small compared to the resonance frequency. Thus, 19640 Hz is set as the resonance frequency. Other equivalent circuit parameters of the GMUPS system can be measured by the impedance analyzer (PV70A, Beijing Banglian, China), and the results are shown in Table 3. After getting these parameters, experiments to explore the effect of driving voltages and magnetic material on the phase lag angle are performed by measuring $X_{\rm ms}$ and $R_{\rm ms}$, since they are critical factors that affect the system's idle vibration amplitude.

4.1 Driving voltage

The effects of driving voltage (peak-to-peak value $V_{\rm pp}$) on the phase lag angle are shown in Fig. 11a. The minimum current frequency and the mechanical resonance frequency decrease with the voltage, but the

Table 3 Equivalent parameters of GMUPS

Parameter	Value
Electrical half-power bandwidth, f_2 - f_1 (Hz)	80
Equivalent mass, m (kg)	0.2
Equivalent inductance, $L_{\rm m}$ (H)	0.2
Equivalent resistance, $R_{\rm m}(\Omega)$	100.5
Equivalent capacitance, C_{m} (nF)	1.03



Fig. 11 Phase lag angle with different driving voltage (a) and phase lag angle with different materials (b)

theoretical analysis in Section 2.5 and demonstrate that the capacitance compensation method is effective not only under no-load but also under load.

phase lag angle changes only slightly with the driving voltage. In the high-frequency dynamic response, the core loss of GMUPS is usually dominated by eddy current loss, while the hysteresis loss accounts for a low proportion and can be ignored (Song et al., 2019). The core loss is proportional to the square of the driving voltage before reaching magnetic saturation. Moreover, the energy loss caused by the skin effect is also proportional to the square of the driving voltage. The total energy consumption of the system is also proportional to the square of the driving voltage. Thus, the proportion of the energy loss caused by the core loss and skin effect to the overall energy consumption is unchanged. Therefore, the driving voltage has little effect on the phase lag angle.

4.2 Material of the magnetic conductive structure

To ensure the closed loop of the internal magnetic circuit of the transducer, a magnetic conductive structure is arranged inside the transducer. Different materials have different core losses and skin effects, resulting in different phase lag angles. The phase lag angle and the frequency difference (Δf) between the mechanical resonance frequency and the minimum current frequency were measured using magnetic powder and ingot iron as magnetic conductive structure materials, respectively. The measurement results are shown in Fig. 11b.

The GMUPS using a magnetic powder core achieves a smaller phase lag angle and less difference between the mechanical resonance frequency and the minimum current frequency. This is because the magnetic powder core material is sintered compared with the ingot iron material. As a result, its iron loss and skin effect are weaker, resulting in less unnecessary energy loss. Thus, the phase lag angle and frequency deviation of GMUPS using the magnetic powder core are smaller than those of ferromagnetic materials. Therefore, we recommend that the magnetic powder core is used as the magnetic conductive material for GMUPS.

5 Conclusions

In this study, the model of optimal compensation capacitance for GMTs with an LCCPT is developed to achieve the maximum energy utilization efficiency. The model stresses the phase lag angle between the mechanical and electrical circuits, while considering the non-negligible loss in energy conversion caused by the core loss and the skin effect in GMM. Idle vibration experiments and machining tests are conducted to verify the developed model. The following conclusions are drawn:

1. The adoption of optimal compensation capacitance shows superior performance for both idle and machining conditions. The system can obtain the maximum amplitude and achieve the highest energy efficiency, while the cutting force is the smallest in the whole process of machining when the optimal compensation capacitance is adopted.

2. The use of LCCPT and the value of the compensation capacitance significantly affect the electrical characteristics of the system but have only a slight effect on the mechanical resonance frequency. Thus, the electrical resonance frequency of the system can be changed independently by the compensation capacitance. The system's performance can be improved by making the electrical resonance frequency closer to the mechanical resonance frequency.

3. The phase lag angle between the electrical circuit and the equivalent mechanical circuit of the system results in a discrepancy between the minimum current frequency and the mechanical resonance frequency. The phase lag angle is directly related to the unnecessary power loss of the system. The driving voltage has little effect on the phase lag angle before reaching magnetic saturation. However, the material properties of the magnetic conductive structure, such as core loss, notably affect the phase lag angle. Therefore, selecting the magnetic conductive material with low loss at high frequency can effectively reduce the phase lag angle.

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Author contributions

Tian LAN made the theoretical derivation and experimental design and processed the corresponding data. Hui-lin ZHOU participated in the theoretical model design. Jian-fu ZHANG helped to make the experiment. Jian-jian WANG wrote the first draft of the manuscript. Ping-fa FENG revised and edited the final version.

Conflict of interest

Tian LAN, Ping-fa FENG, Jian-jian WANG, Jian-fu ZHANG, and Hui-lin ZHOU declare that they have no conflict of interest.

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